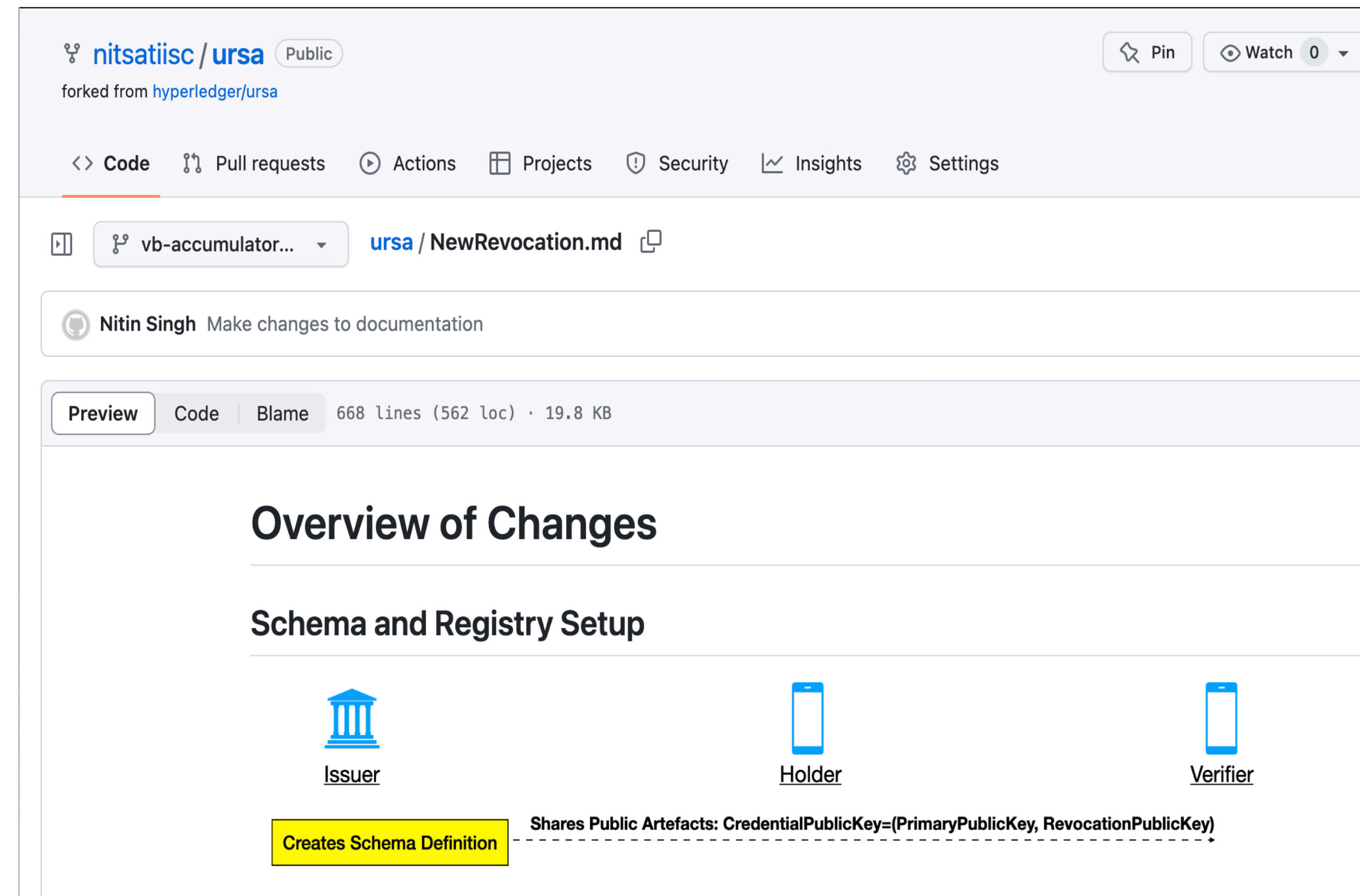


# VB Accumulator Integration in Ursa

- Ursa Fork: <https://github.com/nitsatiisc/ursa.git>
- Branch: [vb-accumulator-changes](#)
- Overview: [NewRevocation.md](#)
- Tests & Benchmarks: [https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test\\_generic\\_interface.rs](https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test_generic_interface.rs)
- VB Scheme: [https://link.springer.com/chapter/10.1007/978-3-030-95312-6\\_17](https://link.springer.com/chapter/10.1007/978-3-030-95312-6_17)



The screenshot shows a GitHub repository page for 'nitsatiisc / ursa' (Public), forked from 'hyperledger/ursa'. The repository has a navigation bar with links for Code, Pull requests, Actions, Projects, Security, Insights, and Settings. The current view is for a commit by Nitin Singh titled 'Make changes to documentation' in the 'vb-accumulator...' branch, specifically for the file 'ursa / NewRevocation.md'. The commit details show 668 lines (562 loc) and 19.8 KB. Below the commit information, there is a section titled 'Overview of Changes' and 'Schema and Registry Setup'. This section includes a diagram with three roles: Issuer (represented by a classical building icon), Holder (represented by a smartphone icon), and Verifier (represented by a smartphone icon). A yellow box labeled 'Creates Schema Definition' is connected to the Issuer role. A dashed arrow points from the Issuer role to the Holder and Verifier roles, with the text 'Shares Public Artefacts: CredentialPublicKey=(PrimaryPublicKey, RevocationPublicKey)' above the arrow.

# Motivation

- To overcome the practical challenges in rolling out existing credential revocation for mass issuers (like New York State) for several million credentials.
- *For example, supporting revocation registries accounting for 20 million credentials would require dissemination of 16GB of public parameters (as tails vectors) to holder devices (hundreds of MB each).*

# Key Advantages

- The Vitto-Biryukov accumulator [1] supports efficient operations (proof, verification, witness update) without requiring dissemination of large public parameters ( **no gigabytes of public parameters** ).
- Verification of non-revocation proof requires **just one pairing** check using modified proof of knowledge on the lines of improved proof of knowledge of the BBS+ signature from [2].

1. **Giuseppe Vitto, Alex Biryukov: Dynamic Universal Accumulator with Batch Update over Bilinear Groups.** CT-RSA 2022.
2. **Jan Camenisch, Manu Drijvers, Anja Lehmann: Anonymous Attestation Using the Strong Diffie Hellman Assumption Revisited.** TRUST 2016.

# **Overview of Key Interactions and Objects**

# Setup



Issuer



Holder



Verifier

Creates Schema Definition

Shares Public Artefacts:  $\text{CredentialPublicKey}=(\text{PrimaryPublicKey}, \text{RevocationPublicKey})$

Creates Initial Registry

Shares Public Artefacts:  $\text{RevocationKeyPublic}$ , Initial Registry State

PrimaryPublicKey

PrimaryPrivateKey

RevocationPublicKey

RevocationPrivateKey

RegistryPublicKey

RegistryPrivateKey

Relevant to all registries

Relevant to specific registry

# Credential Issuance

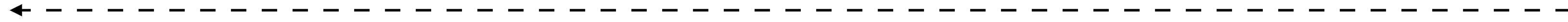


Issuer



Holder

Credential request with blinded attributes



CredentialSignature



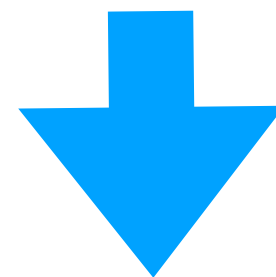
RevocationRegistry

RevocationRegistryDelta

PrimaryCredentialSignature

NonRevocationCredentialSignature

CredentialSignature



Public Update

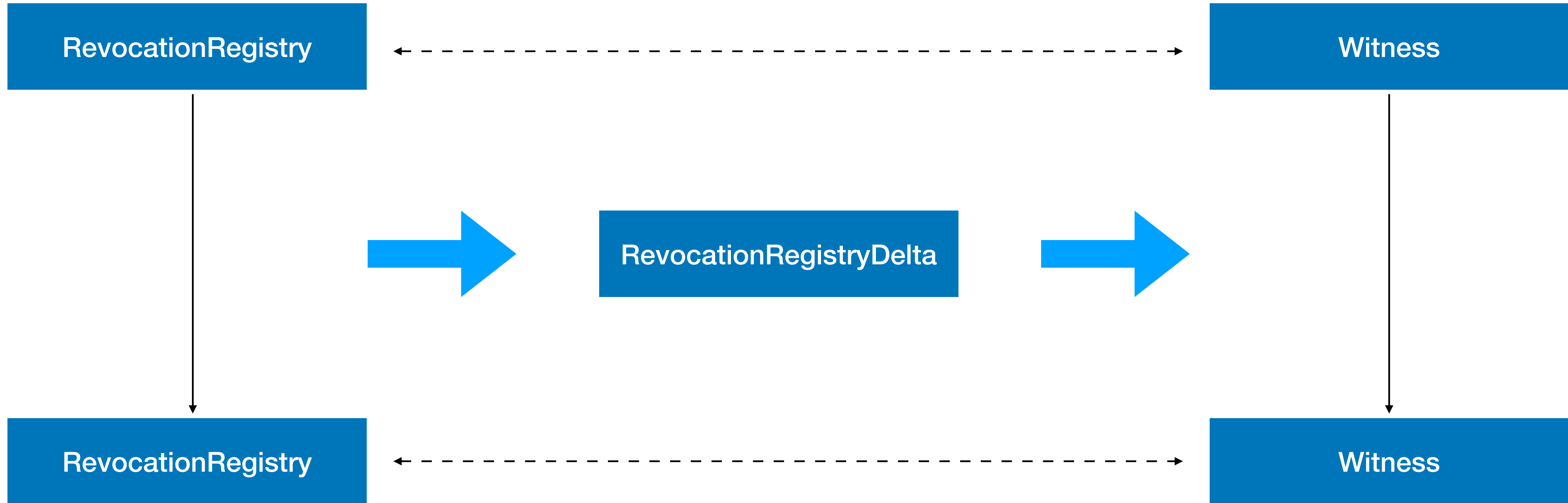
# Witness Management



Issuer

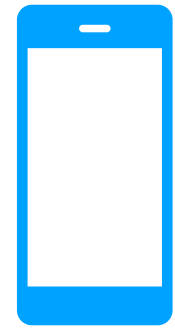


Holder

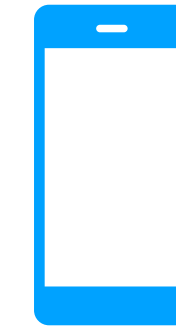
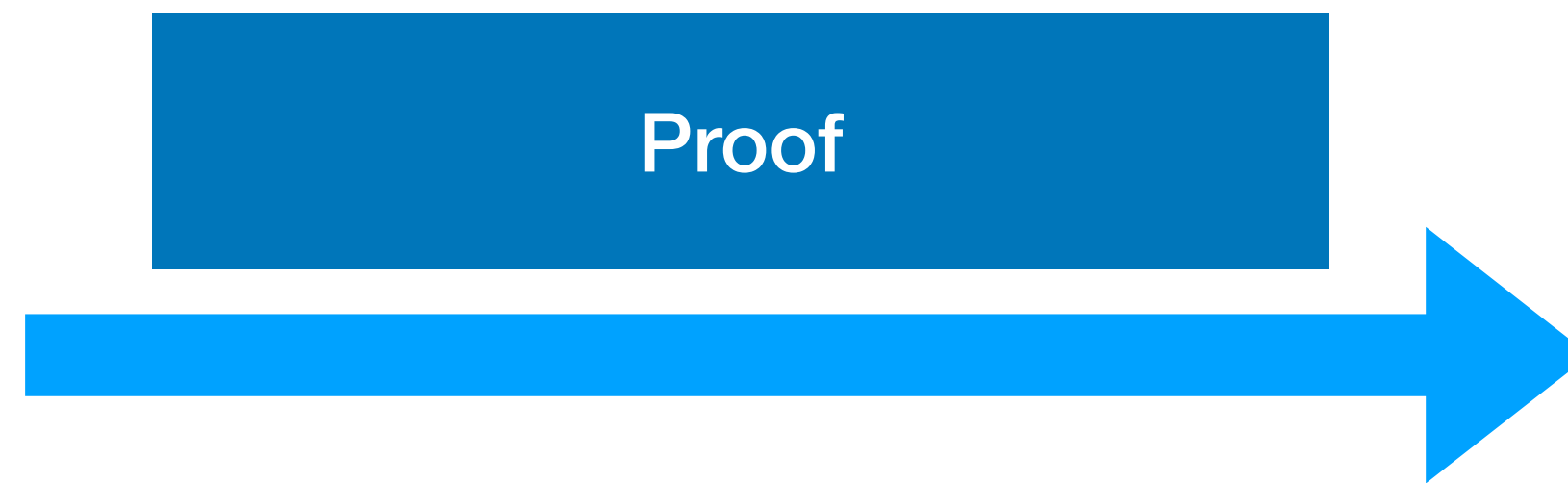
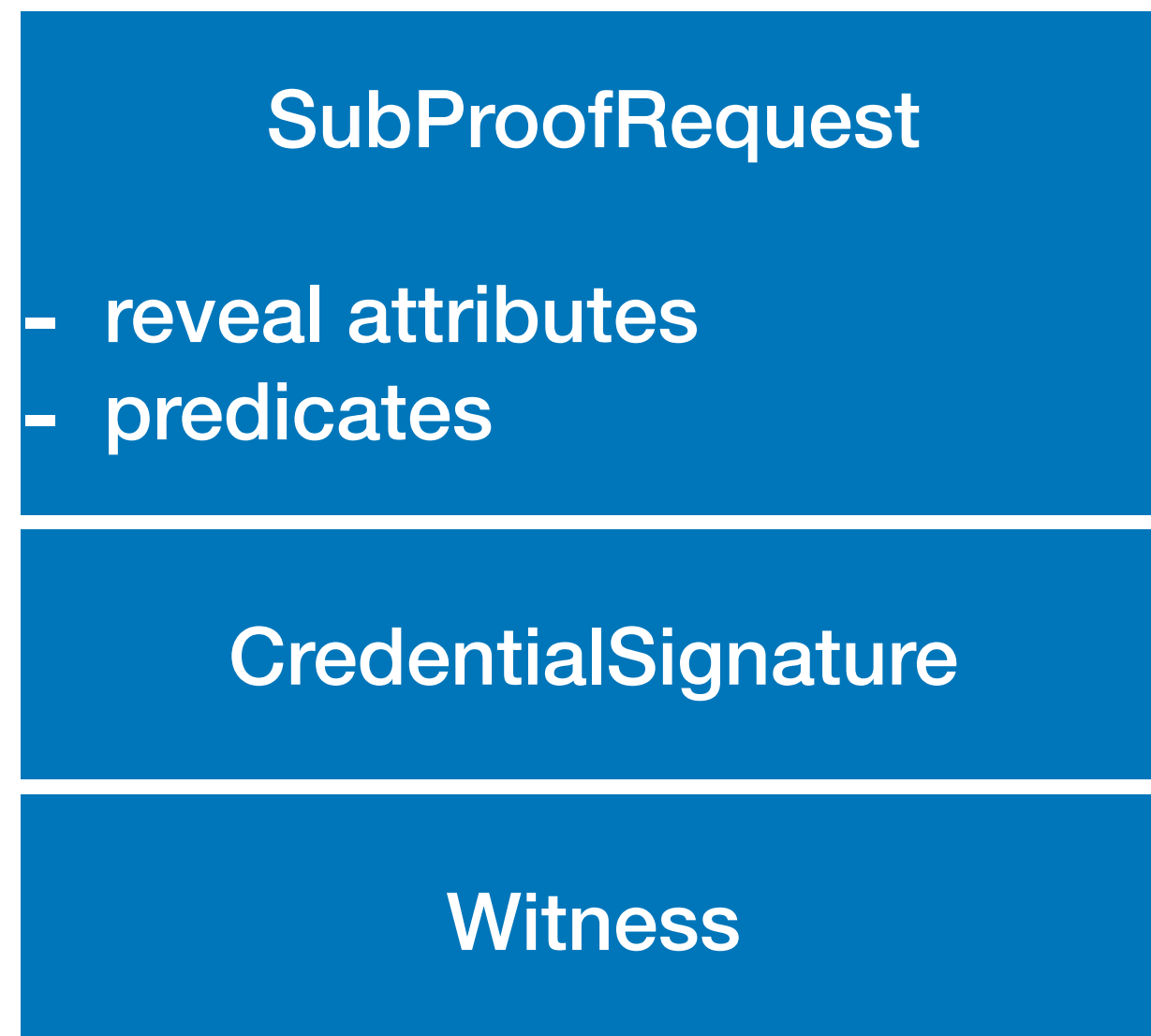


**\*Witness is the part of credential that needs to be continually updated in sync with Revocation Registry**

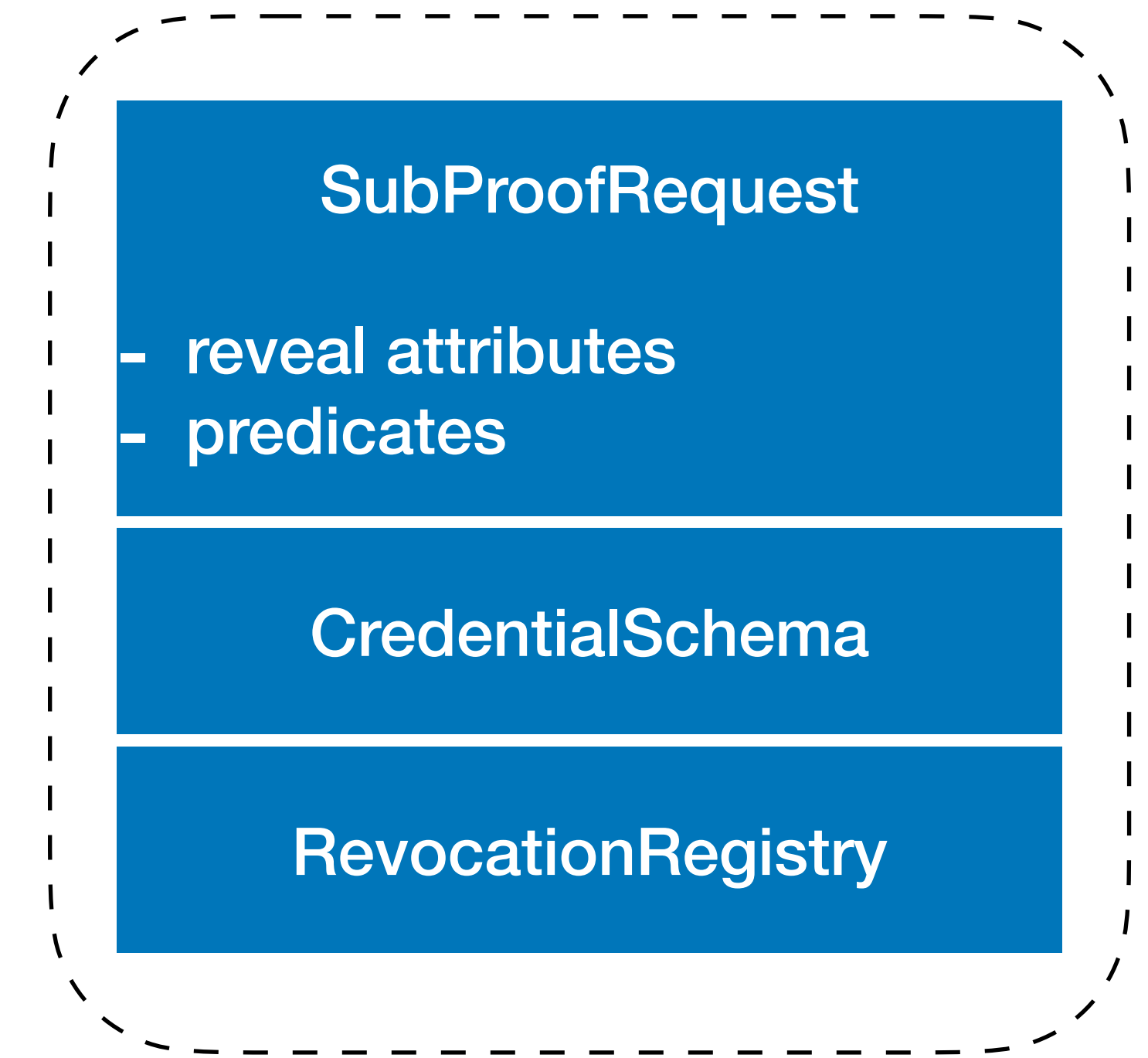
# Proof Presentation



Holder



Verifier



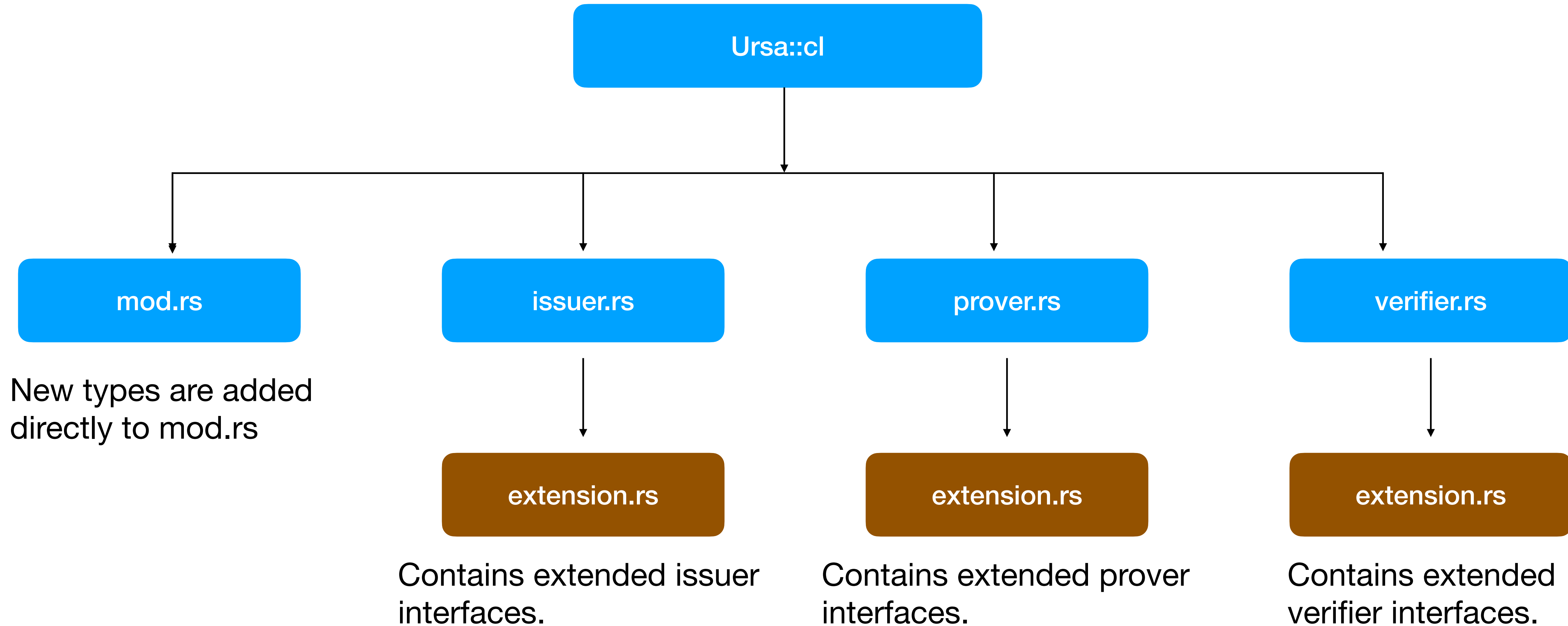
Verifier Policy



# Design Goals

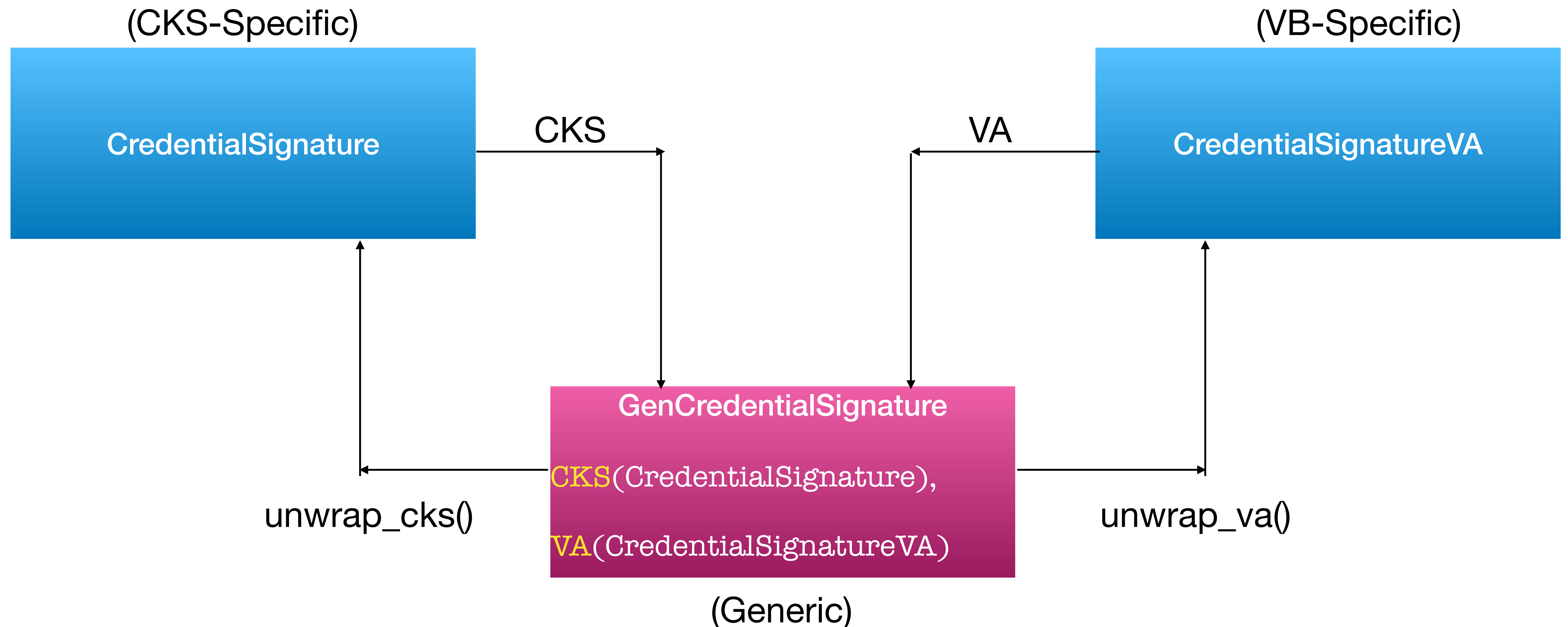
- Backward Compatibility (Strict): Existing artefacts should work as is using existing interfaces. No changes to existing interfaces, or changes affecting them (**Zero changes to existing code**).
- Forward Compatibility (Weak): It should be easy to use artefacts generated using existing interface with newer interface with minimal “wrapper” code.
- General Interface: Interfaces are **revocation-scheme agnostic** as much as possible.

# Overview of changes to libursa CL module



# Implementation : Generic/Wrapper Types

For each type which depends on revocation scheme, introduce a VB-specific type, and a generic type which can represent both.



**Disclaimer/Apology: All the VB-specific types end with VA !!! Mixup between first and second name of second author Alex Biryukov.**

# Implementation: Generic Functions - I

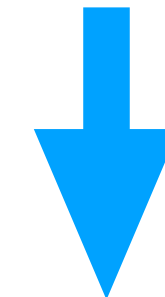
Define analogous functions for the new revocation scheme:

CKS		VA
<pre>pub fn new_credential_def(     credential_schema: &amp;CredentialSchema,     non_credential_schema: &amp;NonCredentialSchema,     support_revocation: bool, ) -&gt; UrsaCryptoResult&lt;(CredentialPublicKey,     CredentialPrivateKey,     CredentialKeyCorrectnessProof, )&gt;</pre>	<pre>&lt;- -- &gt;</pre>	<pre>pub fn new_credential_def_va(     credential_schema: &amp;CredentialSchema,     non_credential_schema: &amp;NonCredentialSchema,     support_revocation: bool ) -&gt; UrsaCryptoResult&lt;(CredentialPublicKeyVA,     CredentialPrivateKeyVA,     CredentialKeyCorrectnessProof )&gt;</pre>

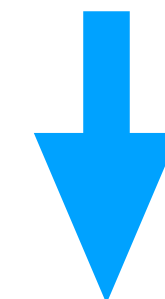
# Implementation: Generic Functions - II

```
pub fn new_revocation_registry_generic(
    cred_pub_key: &GenCredentialPublicKey,
    max_cred_num: u32,
    issuance_by_default: bool,
    max_batch_size: u32
) -> UrsaCryptoResult<(
    GenRevocationKeyPublic,
    GenRevocationKeyPrivate,
    GenRevocationRegistry,
    AuxiliaryParams,
)> {
    match cred_pub_key {
        GenCredentialPublicKey::CKS(cred_pub_key_cks) => {
            let (reg_key_public, reg_key_private, rev_reg, aux_params) =
                Issuer::new_revocation_registry_def(
                    &cred_pub_key_cks,
                    max_cred_num,
                    issuance_by_default
                )?;
            Ok((GenRevocationKeyPublic::CKS(reg_key_public),
                GenRevocationKeyPrivate::CKS(reg_key_private),
                GenRevocationRegistry::CKS(rev_reg),
                AuxiliaryParams::CKS(aux_params)))
        },
        GenCredentialPublicKey::VA(cred_pub_key_va) => {
            let (reg_key_public, reg_key_private, rev_reg, aux_params) =
                Issuer::new_revocation_registry_def_va(
                    &cred_pub_key_va,
                    max_cred_num,
                    max_batch_size
                )?;
            Ok((GenRevocationKeyPublic::VA(reg_key_public),
                GenRevocationKeyPrivate::VA(reg_key_private),
                GenRevocationRegistry::VA(rev_reg),
                AuxiliaryParams::VA(aux_params)
            ))
        },
        _ => Err(err_msg(UrsaCryptoErrorKind::InvalidStructure, "Invalid Credential Public Key"))
    }
}
```

Downgrade generic types to specific types



Delegate to specific function



Upgrade results back to generic types




# Extending presentation interface

Existing	Generic
<pre>pub struct SubProof {   primary_proof: PrimaryProof,   non_revoc_proof: Option&lt;NonRevocProof&gt;, }</pre>	<pre>pub struct GenSubProof {   pub primary_proof: PrimaryProof,   pub non_revoc_proof: Option&lt;GenNonRevocProof&gt;, }</pre>
<pre>pub struct Proof {   pub proofs: Vec&lt;SubProof&gt;,   pub aggregated_proof: AggregatedProof, }</pre>	<pre>pub struct GenProof {   pub proofs: Vec&lt;GenSubProof&gt;,   pub aggregated_proof: AggregatedProof, }</pre>
<pre>pub struct VerifiableCredential {   pub_key: CredentialPublicKey,   sub_proof_request: SubProofRequest,   credential_schema: CredentialSchema,   non_credential_schema: NonCredentialSchema,   rev_key_pub: Option&lt;RevocationKeyPublic&gt;,   rev_reg: Option&lt;RevocationRegistry&gt;, }</pre>	<pre>pub struct GenVerifiableCredential {   pub_key: GenCredentialPublicKey,   sub_proof_request: SubProofRequest,   credential_schema: CredentialSchema,   non_credential_schema: NonCredentialSchema,   rev_key_pub: Option&lt;GenRevocationKeyPublic&gt;,   rev_reg: Option&lt;GenRevocationRegistry&gt;, }</pre>

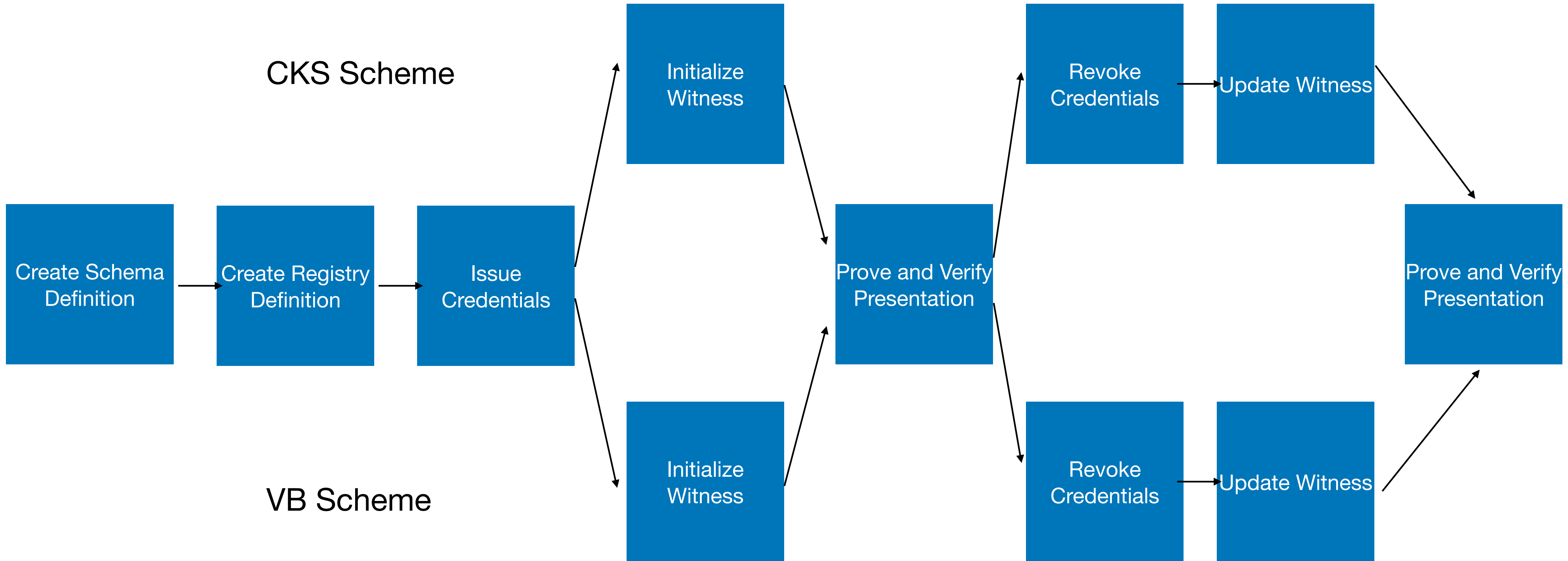
Extend the types to allow different revocation(s)

# Extending Presentation Interface

	CKS (Existing)	Generic (New)
Init Proof	<pre>pub fn add_sub_proof_request(     &amp;mut self,     sub_proof_request: &amp;SubProofRequest,     credential_schema: &amp;CredentialSchema,     non_credential_schema: &amp;NonCredentialSchema,     credential_signature: &amp;CredentialSignature,     credential_values: &amp;CredentialValues,     credential_pub_key: &amp;CredentialPublicKey,     rev_reg: Option&lt;&amp;RevocationRegistry&gt;,     witness: Option&lt;&amp;Witness&gt;, ) -&gt; UrsaCryptoResult&lt;&gt;</pre> 	<pre>pub fn add_sub_proof_request_generic(     &amp;mut self,     sub_proof_request: &amp;SubProofRequest,     credential_schema: &amp;CredentialSchema,     non_credential_schema: &amp;NonCredentialSch     credential_signature: &amp;GenCredentialSign     credential_values: &amp;CredentialValues,     credential_pub_key: &amp;GenCredentialPublic     rev_reg: Option&lt;&amp;GenRevocationRegistry&gt;,     witness: Option&lt;&amp;GenWitness&gt;, ) -&gt; UrsaCryptoResult&lt;&gt;</pre>
Finalize Proof	<pre>pub fn finalize(&amp;self, nonce: &amp;Nonce)     -&gt; UrsaCryptoResult&lt;Proof&gt;</pre>	<pre>pub fn finalize_generic(&amp;self, nonce: &amp;Nonce)     -&gt; UrsaCryptoResult&lt;GenProof&gt;</pre>

Define generic interfaces with generic types

# Tutorial: Complete Workflow Functions



Detailed examples for complete workflows in tutorials module @ [https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test\\_generic\\_interface.rs](https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test_generic_interface.rs)



# Benchmarks

Issuer	CKS(s)	VA(s)
Gen Registry (100K)	126.2	52.7
Issue Credential	0.11	0.13
Issue Update(100)	0.002	0.02

Holder	CKS(ms)	VA(ms)
Init Witness(100K)	250	0
Update Witness(100)	0.0	1
Proof	53	37

Verifier	CKS(ms)	VA(ms)
Verify	49	26

Tests and benchmarks @: [https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test\\_generic\\_interface.rs](https://github.com/nitsatiisc/ursa/blob/vb-accumulator-changes/libursa/tests/test_generic_interface.rs)

# Custom Modifications to VB protocol

- Improved proof of knowledge of the non-revocation witness based on improved PoK for BBS+ signature in [2]. Reduces pairing checks for the verifier from  $\sim 10$  to 1. Results in about 45% faster proving and verification on average.
- Maintain polynomials as evaluations:  $f(x) \equiv \langle f(1), \dots, f(d) \rangle$  and changes to protocol to work with this representation.

**Questions?**

# Vitto-Biryukov Accumulator



$\alpha$

Registry Private State:  $\alpha, Y_0 = \{\beta_1, \dots, \beta_N\}$

Accumulated Set:  $Y_V = \{y_1, \dots, y_k\}$

Accumulator Value:  $V$

$$V = \left( \prod_{z \in Y_0 \cup Y_V} (\alpha + z) \right) \cdot P$$

\* The accumulated set corresponds to revoked elements

# Non Membership Witness

For  $y$  not in the accumulated set, the Issuer issues a non-membership witness  $w_y = (C, d)$  as:

$$C = \frac{f_V(\alpha) - f_V(-y)}{y + \alpha} \cdot P, \quad d = f_V(-y)$$

where

$$f_V(x) = \prod_{z \in Y_0 \cup Y_V} (x + z)$$

We note that  $d$  is non-zero when  $y$  is not in the set. Also note that  $V = f_V(\alpha) \cdot P$

# Batch Update

$$(Y_V, V) \xrightarrow{Y = \{y_1, \dots, y_n\}} (Y_{V'}, V')$$

$$w_y = (C, d) \xrightarrow{?} w'_y = (C', d')$$

$$d_A(x) = \prod_{i=1}^n (x - y_i)$$

$$v_A(x) = \sum_{s=1}^n \left( \prod_{i=1}^{s-1} (y_i + \alpha) \prod_{j=s+1}^n (y_i - x) \right)$$

$$d' = d_A(y) \cdot d$$

$$C' = d_A(y) \cdot C + v_A(y) \cdot V$$

# Batch Update -II

The issuer cannot publish polynomial  $v_A(x)$  in plain-text, as it can leak  $\alpha$ . Thus as part of batch update protocol, issuer publishes:

$$\Omega = (c_0 \cdot V, c_1 \cdot V, \dots, c_n \cdot V)$$

Where:  $v_A(x) = c_0 + c_1x + \dots + c_nx^n$

From the above update, the holder can locally compute  $v_A(y) \cdot V$  as the following scalar product:

$$v_A(y) \cdot V = \langle (1, y, y^2, \dots, y^n), \Omega \rangle$$

# Modified Batch Update

The issuer cannot publish polynomial  $v_A(x)$  in plain-text, as it can leak  $\alpha$ . Thus as part of batch update protocol, issuer publishes:

$$\Omega = (v_A(\omega_0) \cdot V, v_A(\omega_1) \cdot V, \dots, v_A(\omega_n) \cdot V)$$

Where:  $\omega_0, \dots, \omega_n$  are fixed.

From the above update, the holder can locally compute  $v_A(y) \cdot V$  as the following scalar product:

$$v_A(y) \cdot V = \langle (\ell_0, \dots, \ell_n), \Omega \rangle$$

In the above  $\ell_0, \dots, \ell_n$  are Lagrangian coefficients such that:

$$v_A(y) = \sum_{i=0}^n \ell_i v_A(\omega_i)$$